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# Symmetric Key Cryptography

## Chapter 3

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**IS433 Information Security**

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# Chapter 3:

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## Symmetric Key Crypto

The chief forms of beauty are order and symmetry...  
— Aristotle

“You boil it in sawdust: you salt it in glue:  
You condense it with locusts and tape:  
Still keeping one principal object in view —  
To preserve its symmetrical shape.”  
— Lewis Carroll, *The Hunting of the Snark*

# Symmetric Key Crypto

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- **Stream cipher — based on one-time pad**
  - Except that key is **relatively short**
  - Key is stretched into a long **keystream**
  - Keystream is used just like a one-time pad (advantage  
Provably secure but Key is too long )
- **Block cipher — based on codebook concept**
  - Block cipher key determines a codebook
  - Each key yields a different codebook
  - Employs both “confusion” and “diffusion”

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# Stream Ciphers



# Stream Ciphers

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- Once upon a time, not so very long ago, stream ciphers were the **king** of crypto
- Today, **not as popular** as block ciphers
- We'll discuss two stream ciphers...
- **A5/1**
  - Based on shift registers
  - Used in GSM mobile phone system
- **RC4**
  - Based on a changing lookup table
  - Used many places

# A5/1: Shift Registers

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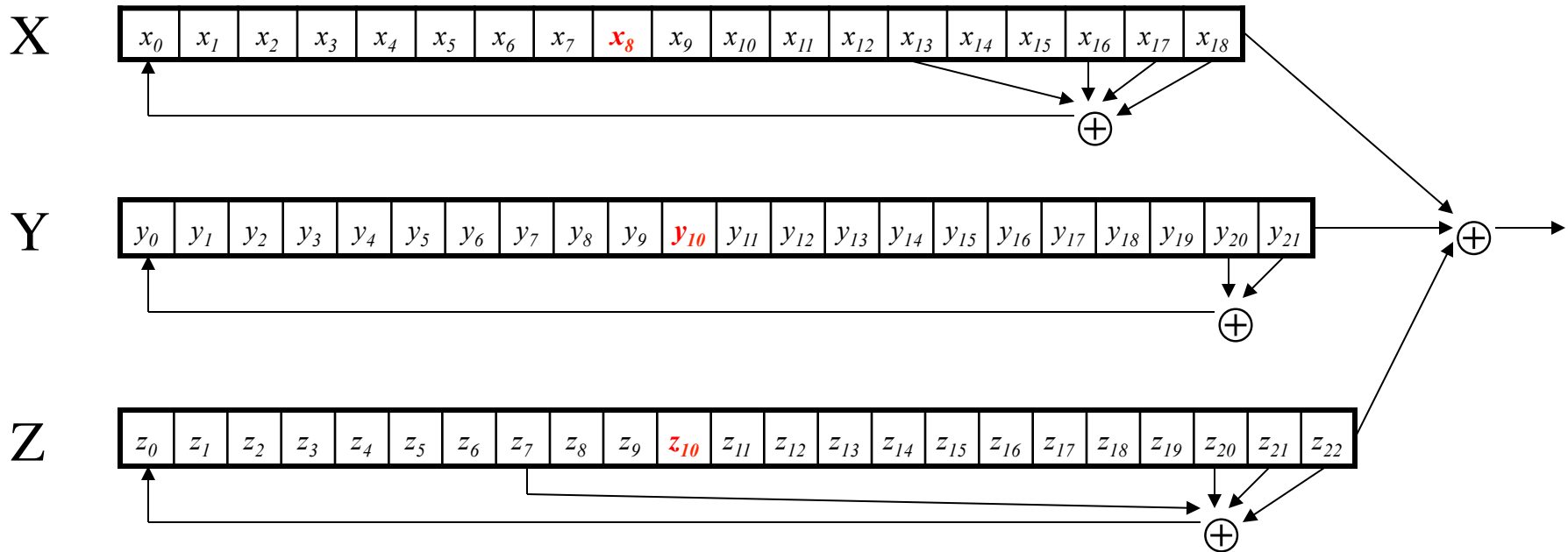
- A5/1 uses 3 *shift registers (LFSR)*
  - X: 19 bits ( $x_0, x_1, x_2, \dots, x_{18}$ )
  - Y: 22 bits ( $y_0, y_1, y_2, \dots, y_{21}$ )
  - Z: 23 bits ( $z_0, z_1, z_2, \dots, z_{22}$ )

# A5/1: Keystream

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- At each step:  $m = \text{maj}(x_8, y_{10}, z_{10})$ 
  - Examples:  $\text{maj}(0,1,0) = 0$  and  $\text{maj}(1,1,0) = 1$
- If  $x_8 = m$  then *Xsteps*
  - $t = x_{13} \oplus x_{16} \oplus x_{17} \oplus x_{18}$
  - $x_i = x_{i-1}$  for  $i = 18, 17, \dots, 1$  and  $x_0 = t$
- If  $y_{10} = m$  then *Ysteps*
  - $t = y_{20} \oplus y_{21}$
  - $y_i = y_{i-1}$  for  $i = 21, 20, \dots, 1$  and  $y_0 = t$
- If  $z_{10} = m$  then *Zsteps*
  - $t = z_7 \oplus z_{20} \oplus z_{21} \oplus z_{22}$
  - $z_i = z_{i-1}$  for  $i = 22, 21, \dots, 1$  and  $z_0 = t$
- Keystreambit is  $x_{18} \oplus y_{21} \oplus z_{22}$

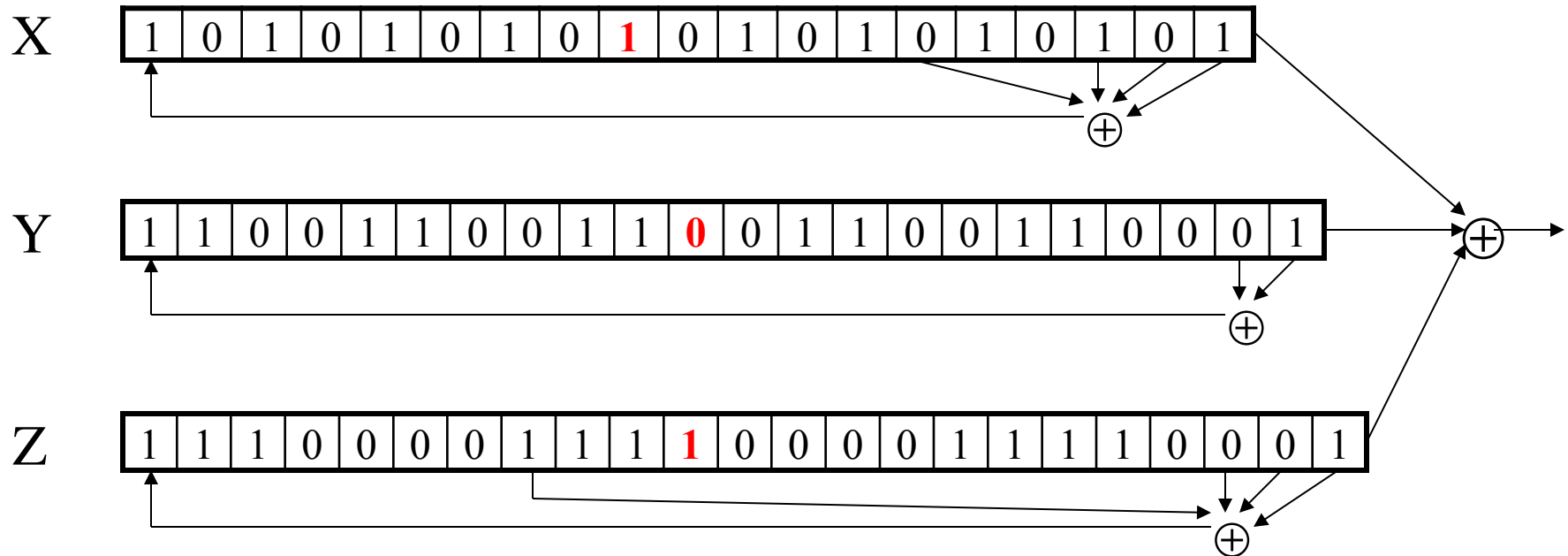
# A5/1



- Each variable here is a single bit
- Key is used as **initial fill** of registers
- Each register steps (**OR NOT**) based on  $\text{maj}(x_8, y_{10}, z_{10})$
- Key stream bit is XOR of rightmost bits of registers



# A5/1



- In this example,  $m = \text{maj}(x_8, y_{10}, z_{10}) = \text{maj}(\mathbf{1}, \mathbf{0}, \mathbf{1}) = \mathbf{1}$
- Register X steps, Y does not step, and Z steps
- Keystream bit is XOR of right bits of registers
- Here, a single keystream bit will be  $0 \oplus 1 \oplus 0 = 1$

# Shift Register Crypto

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- Shift register crypto **efficient in hardware**
- Often, slow if implement in software
- In the past, very popular
- Today, more is done in software due to fast processors
- Shift register crypto still used some
  - Resource-constrained devices

# RC4

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- A self-modifying lookup table
- Table always contains a permutation of the byte values 0,1,...,255
- Initialize the permutation using key
- At each step, RC4 does the following
  - Swaps elements in current lookup table
  - Selects a key stream byte from table
- Each step of RC4 produces a byte
  - Efficient in software
- Each step of A5/1 produces only a bit
  - Efficient in hardware

# RC4 Initialization

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- Here two things we need to do:
- (initialize the key then issue the key)
- $S[]$  is permutation of  $0, 1, \dots, 255$   $key[]$  contains  $N$  bytes of key

```
(1)  for i = 0 to 255
      S[i] = i
      K[i] = key[i (mod N)]
    next i
```

```
      j = 0
(2)  for i = 0 to 255
      j = (j + S[i] + K[i]) mod 256
      swap(S[i], S[j])
    next i
    i = j = 0
```

# RC4 Keystream

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- For each keystream byte, swap elements in table and select byte

$i = (i + 1) \bmod 256$

$j = (j + S[i]) \bmod 256$

$\text{swap}(S[i], S[j])$

$t = (S[i] + S[j]) \bmod 256$

$\text{keystreamByte} = S[t]$

- Use keystream bytes like a one-time pad
- **Note:** first 256 bytes should be discarded
  - Otherwise, related key attack exists

# Stream Ciphers

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- Stream ciphers were popular in the past
  - Efficient in hardware
  - Speed was needed to keep up with voice, etc.
  - Today, processors are fast, so software-based crypto is usually more than fast enough
- Future of stream ciphers?
  - Shamir declared “the death of stream ciphers”
  - May be greatly exaggerated...

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# Block Ciphers



# (Iterated) Block Cipher

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- Plaintext and ciphertext consist of fixed-sized blocks
- Ciphertext obtained from plaintext by iterating a **round function**
- Input to round function consists of **key** and **output** of previous round
- Usually implemented in **software**



# Feistel Cipher: Encryption

- **Feistel cipher** is a type of block cipher, not a specific block cipher (general approach to build a block)
- Split **plaintext block** into left and right halves:

$$P = (L_0, R_0)$$

- For each round  $i = 1, 2, \dots, n$ , compute

$$L_i = R_{i-1}$$

$$R_i = L_{i-1} \oplus F(R_{i-1}, K_i)$$

where  $F$  is **round function** and  $K_i$  is **subkey**

- Ciphertext:  $C = (L_n, R_n)$

# Feistel Cipher: Decryption

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- Start with ciphertext  $C = (L_n, R_n)$
- For each round  $i = n, n-1, \dots, 1$ , compute

$$R_{i-1} = L_i$$

$$L_{i-1} = R_i \oplus F(R_{i-1}, K_i)$$

where  $F$  is round function and  $K_i$  is subkey for round  $i$

- Plaintext:  $P = (L_0, R_0)$
- Formula “works” for any function  $F$ 
  - But only secure for certain functions  $F$

# Data Encryption Standard

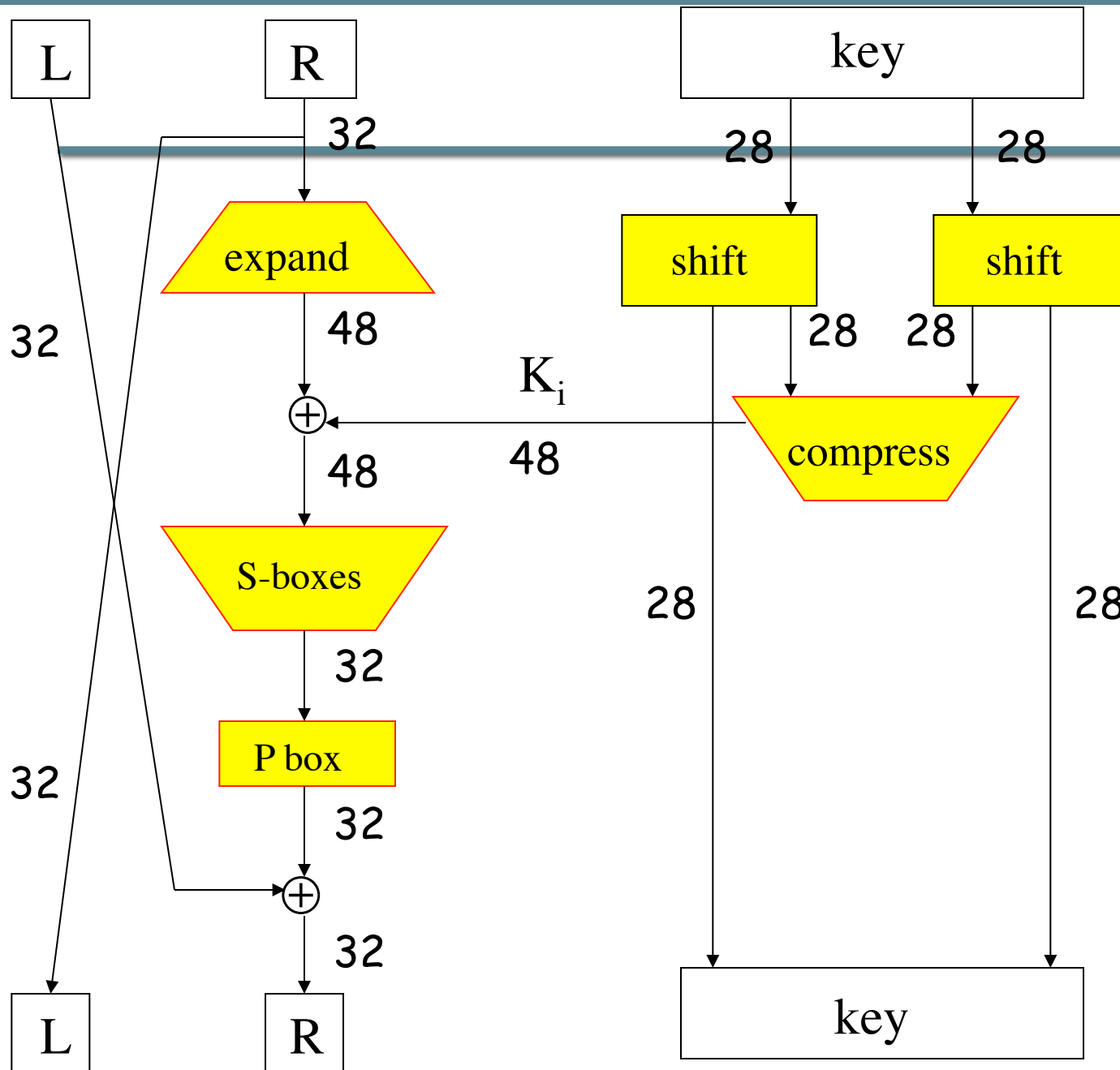
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- **DES** developed in 1970's
- Based on IBM's Lucifer cipher
- DES was U.S. government standard
- DES development was controversial
  - NSA secretly involved
  - Design process was secret
  - Key length reduced from 128 to 56 bits
  - Subtle changes to Lucifer algorithm

# DES Numerology

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- DES is a Feistel cipher with...
  - 64 bit block length
  - 56 bit key length (the 8 bits can be used for error detection)
  - 16 rounds
  - 48 bits of key used each round (subkey)
- Each round is simple (for a block cipher)
- Security depends heavily on “S-boxes”
  - Each S-boxes maps 6 bits to 4 bits



One  
Round  
of  
DES

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[https://www.youtube.com/  
watch?v=\\_RRrOwOjeHg](https://www.youtube.com/watch?v=_RRrOwOjeHg)

# DES Expansion Permutation

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- Input 32 bits

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31

- Output 48 bits

31	0	1	2	3	4	3	4	5	6	7	8
7	8	9	10	11	12	11	12	13	14	15	16
15	16	17	18	19	20	19	20	21	22	23	24
23	24	25	26	27	28	27	28	29	30	31	0

# DES S-box

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- 8 “substitution boxes” or S-boxes
- Each S-box maps 6 bits to 4 bits
- S-box number 1

Suppose we have the input (0,1,2,3,4,5)

input bits (0,5)

↓ input bits (1,2,3,4)

	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111
00	1110	0100	1101	0001	0010	1111	1011	1000	0011	1010	0110	1100	0101	1001	0000	0111
01	0000	1111	0111	0100	1110	0010	1101	0001	1010	0110	1100	1011	1001	0101	0011	1000
10	0100	0001	1110	1000	1101	0110	0010	1011	1111	1100	1001	0111	0011	1010	0101	0000
11	1111	1100	1000	0010	0100	1001	0001	0111	0101	1011	0011	1110	1010	0000	0110	1101



# DES P-box

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- Input 32 bits

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31

- Output 32 bits

15	6	19	20	28	11	27	16	0	14	22	25	4	17	30	9
1	7	23	13	31	26	2	8	18	12	29	5	21	10	3	24

# DES Subkey

---

- 56 bit DES key, numbered 0,1,2,...,55
- Left half key bits, **LK**

49	42	35	28	21	14	7
0	50	43	36	29	22	15
8	1	51	44	37	30	23
16	9	2	52	45	38	31

- Right half key bits, **RK**

55	48	41	34	27	20	13
6	54	47	40	33	26	19
12	5	53	46	39	32	25
18	11	4	24	17	10	3

# DES Subkey

---

- For rounds  $i=1, 2, \dots, 16$ 
  - Let  $LK = (LK \text{ circular shift left by } r_i)$
  - Let  $RK = (RK \text{ circular shift left by } r_i)$
  - Left half of subkey  $K_i$  is of  $LK$  bits

13	16	10	23	0	4	2	27	14	5	20	9
22	18	11	3	25	7	15	6	26	19	12	1

- Right half of subkey  $K_i$  is  $RK$  bits

12	23	2	8	18	26	1	11	22	16	4	19
15	20	10	27	5	24	17	13	21	7	0	3

# DES Subkey

---

- For rounds 1, 2, 9 and 16 the shift  $r_i$  is 1, and in all other rounds  $r_i$  is 2
- Bits 8,17,21,24 of LK omitted each round
- Bits 6,9,14,25 of RK omitted each round
- **Compression permutation** yields 48 bit subkey  $K_i$  from 56 bits of LK and RK
- **Key schedule** generates subkey

# DES Last Word (Almost)

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- An initial permutation before round 1
- Halves are swapped after last round
- A final permutation (inverse of initial perm) applied to  $(R_{16}, L_{16})$
- None of this serves security purpose

# Security of DES

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- Security depends heavily on **S-boxes**
  - Everything else in DES is linear (**easy to solve**)
- Thirty+ years of intense analysis has revealed no “back door”
- Attacks, essentially exhaustive key search
- **Inescapable conclusions**
  - Designers of DES knew what they were doing
  - Designers of DES were way ahead of their time

# Block Cipher Notation

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- $P$  = plaintext block
- $C$  = ciphertext block
- Encrypt  $P$  with key  $K$  to get ciphertext  $C$ 
  - $C = E(P, K)$
- Decrypt  $C$  with key  $K$  to get plaintext  $P$ 
  - $P = D(C, K)$
- Note:  $P = D(E(P, K), K)$  and  $C = E(D(C, K), K)$ 
  - But  $P \neq D(E(P, K_1), K_2)$  and  $C \neq E(D(C, K_1), K_2)$  when  $K_1 \neq K_2$

# Triple DES

---

- Today, 56 bit DES key is too small
  - Exhaustive key search is feasible
- But DES is everywhere, so what to do?
- **Triple DES** or **3DES** (112 bit key)
  - $C = E(D(E(P, K_1), K_2), K_1)$
  - $P = D(E(D(C, K_1), K_2), K_1)$
- Why Encrypt-Decrypt-Encrypt with 2 keys?
  - Backward compatible:  $E(D(E(P, K), K), K) = E(P, K)$
  - And 112 bits is enough



# 3DES

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- Why not  $C = E(E(P, K), K)$  ?
  - Trick question --- it's still just 56 bit key
- Why not  $C = E(E(P, K_1), K_2)$  ?
- A (semi-practical) **known plaintext** attack
  - Pre-compute table of  $E(P, K_1)$  for every possible key  $K_1$  (resulting table has  $2^{56}$  entries)
  - Then for each possible  $K_2$  compute  $D(C, K_2)$  until a match in table is found
  - When match is found, have  $E(P, K_1) = D(C, K_2)$
  - Result gives us keys:  $C = E(E(P, K_1), K_2)$

# Advanced Encryption Standard

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- Replacement for DES
- AES competition (late 90's)
  - NSA openly involved
  - Transparent process
  - Many strong algorithms proposed
  - Rijndael Algorithm ultimately selected (pronounced like “Rain Doll” or “Rhine Doll”)
- Iterated block cipher (like DES)
- Not a Feistel cipher (unlike DES)

Feistel cipher is easy to decrypt if you know the key  
(because of XOR)

# AES Overview

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- **Block size:** 128 bits (others in Rijndael)
- **Key length:** 128, 192 or 256 bits (**independent** of block size)
- 10 to 14 rounds (**depends** on key length)
- Each round uses 4 functions (3 “layers”)
  - **ByteSub** (nonlinear layer)
  - **ShiftRow** (linear mixing layer)
  - **MixColumn** (nonlinear layer)
  - **AddRoundKey** (key addition layer)

# AES ByteSub

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- Treat 128 bit block as 4x6 byte array

$$\begin{bmatrix} a_{00} & a_{01} & a_{02} & a_{03} \\ a_{10} & a_{11} & a_{12} & a_{13} \\ a_{20} & a_{21} & a_{22} & a_{23} \\ a_{30} & a_{31} & a_{32} & a_{33} \end{bmatrix} \longrightarrow \text{ByteSub} \longrightarrow \begin{bmatrix} b_{00} & b_{01} & b_{02} & b_{03} \\ b_{10} & b_{11} & b_{12} & b_{13} \\ b_{20} & b_{21} & b_{22} & b_{23} \\ b_{30} & b_{31} & b_{32} & b_{33} \end{bmatrix} .$$

- ByteSub is AES's “S-box”
- Can be viewed as nonlinear (but invertible) composition of two math operations

# AES “S-box”

Last 4 bits of input

First 4  
bits of  
input

	0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

# AES ShiftRow

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- Cyclic shift rows

$$\begin{bmatrix} a_{00} & a_{01} & a_{02} & a_{03} \\ a_{10} & a_{11} & a_{12} & a_{13} \\ a_{20} & a_{21} & a_{22} & a_{23} \\ a_{30} & a_{31} & a_{32} & a_{33} \end{bmatrix} \longrightarrow \text{ShiftRow} \longrightarrow \begin{bmatrix} a_{00} & a_{01} & a_{02} & a_{03} \\ a_{11} & a_{12} & a_{13} & a_{10} \\ a_{22} & a_{23} & a_{20} & a_{21} \\ a_{33} & a_{30} & a_{31} & a_{32} \end{bmatrix}$$

# AES MixColumn

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- Invertible, linear operation applied to each column

$$\begin{bmatrix} a_{0i} \\ a_{1i} \\ a_{2i} \\ a_{3i} \end{bmatrix} \longrightarrow \text{MixColumn} \longrightarrow \begin{bmatrix} b_{0i} \\ b_{1i} \\ b_{2i} \\ b_{3i} \end{bmatrix} \quad \text{for } i = 0, 1, 2, 3$$

- Implemented as a (big) lookup table

# AES AddRoundKey

---

## □ XOR subkey with block

$$\begin{bmatrix} a_{00} & a_{01} & a_{02} & a_{03} \\ a_{10} & a_{11} & a_{12} & a_{13} \\ a_{20} & a_{21} & a_{22} & a_{23} \\ a_{30} & a_{31} & a_{32} & a_{33} \end{bmatrix} \oplus \begin{bmatrix} k_{00} & k_{01} & k_{02} & k_{03} \\ k_{10} & k_{11} & k_{12} & k_{13} \\ k_{20} & k_{21} & k_{22} & k_{23} \\ k_{30} & k_{31} & k_{32} & k_{33} \end{bmatrix} = \begin{bmatrix} b_{00} & b_{01} & b_{02} & b_{03} \\ b_{10} & b_{11} & b_{12} & b_{13} \\ b_{20} & b_{21} & b_{22} & b_{23} \\ b_{30} & b_{31} & b_{32} & b_{33} \end{bmatrix}$$

Block

Subkey

- RoundKey (subkey) determined by **key schedule** algorithm



# AES Decryption

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- To decrypt, process must be **invertible**
- Inverse of MixAddRoundKey is easy, since “ $\oplus$ ” is its own inverse
- MixColumn is invertible (inverse is also implemented as a lookup table)
- Inverse of ShiftRow is easy (cyclic shift the other direction)
- ByteSub is invertible (inverse is also implemented as a lookup table)

# Symmetric key crypto

Stream Cipher	Block Cipher
A5\1	Feistel
RC4	DES
	AES
	TEA

	Key	Text	Round
DES	56	64	16
3DES	112	112	3Triple each 16 round
AES	128,192,256	128	10-14
TEA	128	64	variable

---

# Block Cipher Modes

# Multiple Blocks

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- How to encrypt multiple blocks?
- Do we need a new key for each block?
  - As bad as (or worse than) a one-time pad!
- Encrypt each block independently?
- Make encryption depend on previous block?
  - That is, can we “chain” the blocks together?
- How to handle partial blocks?
  - We won't discuss this issue

# Modes of Operation

---

- Many modes — we discuss 3 most popular
- Electronic Codebook (**ECB**) mode
  - Encrypt each block independently
  - Most obvious, but has a serious weakness
- Cipher Block Chaining (**CBC**) mode
  - Chain the blocks together
  - More secure than ECB, virtually no extra work
- Counter Mode (**CTR**) mode
  - Block ciphers acts like a stream cipher
  - Popular for random access

# ECB Mode

---

- Notation:  $C = E(P, K)$
- Given plaintext  $P_0, P_1, \dots, P_m, \dots$
- Most obvious way to use a block cipher:

## Encrypt

$$C_0 = E(P_0, K)$$

$$C_1 = E(P_1, K)$$

$$C_2 = E(P_2, K) \quad \dots$$

## Decrypt

$$P_0 = D(C_0, K)$$

$$P_1 = D(C_1, K)$$

$$P_2 = D(C_2, K) \quad \dots$$

- For fixed key  $K$ , this is “electronic” version of a codebook cipher (without additive)
  - With a different codebook for each key

# ECB Cut and Paste

---

- Suppose plaintext is

Alice digs Bob. Trudy digs Tom.

- Assuming 64-bit blocks and 8-bit ASCII:

$P_0$  = “Alice di”,  $P_1$  = “gs Bob. ”,

$P_2$  = “Trudy di”,  $P_3$  = “gs Tom. ”

- Ciphertext:  $C_0, C_1, C_2, C_3$
- Trudy cuts and pastes:  $C_0, C_3, C_2, C_1$
- Decrypts as

Alice digs Tom. Trudy digs Bob.



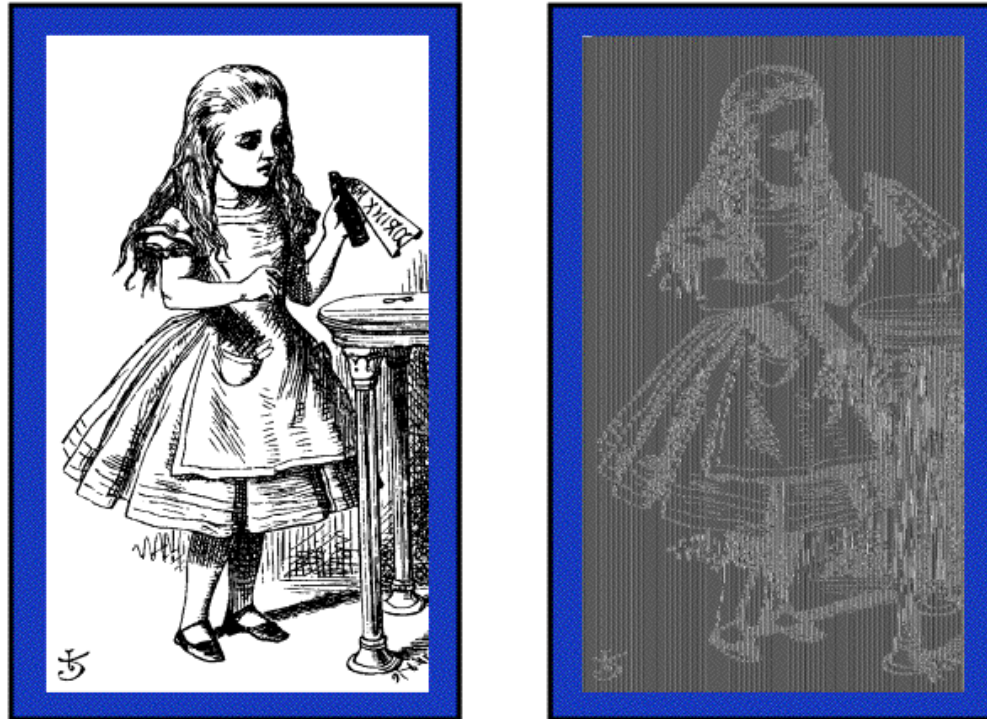
# ECB Weakness

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- Suppose  $P_i = P_j$
- Then  $C_i = C_j$  and Trudy knows  $P_i = P_j$
- This gives Trudy some information, even if she does not know  $P_i$  or  $P_j$
- Trudy might know  $P_i$
- Is this a serious issue?

# Alice Hates ECB Mode

- Alice's uncompressed image, and ECB encrypted (TEA)



- ❑ Why does this happen?
- ❑ Same plaintext yields same ciphertext!

# CBC Mode

---

- Blocks are “chained” together
- A random initialization vector, or IV, is required to initialize CBC mode
- IV is random, but not secret

## Encryption

$$\begin{aligned}C_0 &= E(\text{IV} \oplus P_0, K), \\C_1 &= E(C_0 \oplus P_1, K), \\C_2 &= E(C_1 \oplus P_2, K), \dots\end{aligned}$$

## Decryption

$$\begin{aligned}P_0 &= \text{IV} \oplus D(C_0, K), \\P_1 &= C_0 \oplus D(C_1, K), \\P_2 &= C_1 \oplus D(C_2, K), \dots\end{aligned}$$

- Analogous to classic codebook *with additive*

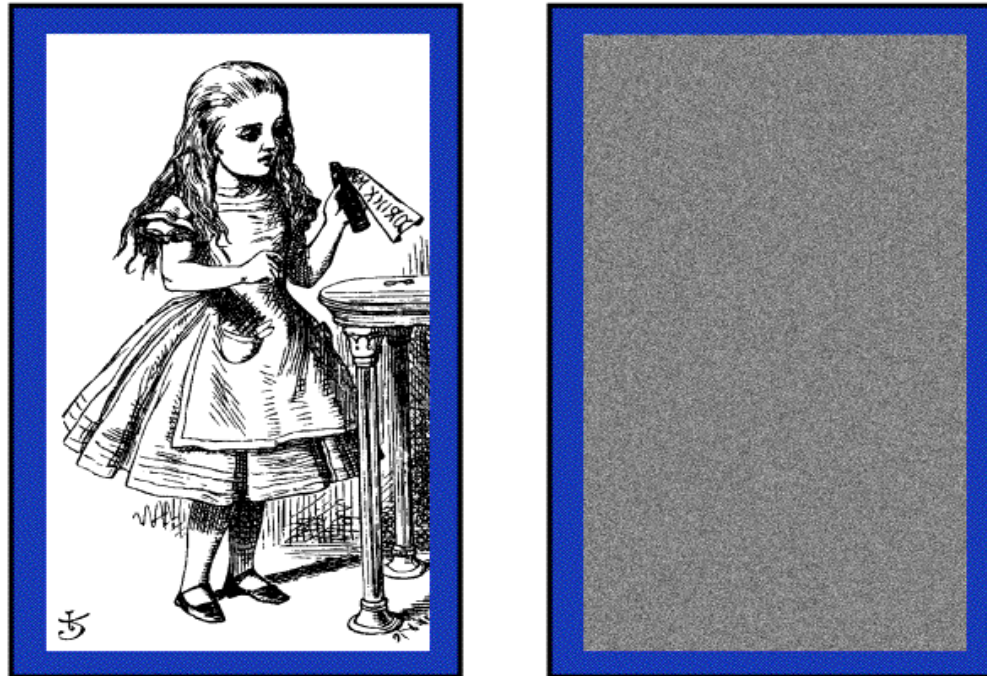
# CBC Mode

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- Identical plaintext blocks yield different ciphertext blocks — this is good!
- If  $C_1$  is garbled to, say,  $G$  then
$$P_1 \neq C_0 \oplus D(G, K), P_2 \neq G \oplus D(C_2, K)$$
- But  $P_3 = C_2 \oplus D(C_3, K), P_4 = C_3 \oplus D(C_4, K), \dots$
- Automatically recovers from errors!
- Cut and paste is still possible, but more complex (and will cause garbles)

# Alice Likes CBC Mode

- Alice's uncompressed image, Alice CBC encrypted (TEA)



- ❑ Why does this happen?
- ❑ Same plaintext yields different ciphertext!

# Counter Mode (CTR)

---

- CTR is popular for random access
- Use block cipher like a stream cipher

## Encryption

$$C_0 = P_0 \oplus E(\text{IV}, K),$$

$$C_1 = P_1 \oplus E(\text{IV}+1, K),$$

$$C_2 = P_2 \oplus E(\text{IV}+2, K), \dots$$

## Decryption

$$P_0 = C_0 \oplus E(\text{IV}, K),$$

$$P_1 = C_1 \oplus E(\text{IV}+1, K),$$

$$P_2 = C_2 \oplus E(\text{IV}+2, K), \dots$$

- CBC can also be used for random access
  - With a significant limitation...

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# Integrity

# Data Integrity

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- **Integrity**— detect unauthorized writing (i.e., modification of data)
- Example: Inter-bank fund transfers
  - Confidentiality may be nice, integrity is critical
- Encryption provides **confidentiality** (prevents unauthorized disclosure)
- Encryption alone does **not** provide integrity
  - One-time pad, ECB cut-and-paste, etc.



# MAC

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- Message Authentication Code (MAC)
  - Used for data **integrity**
  - Integrity **not** the same as confidentiality
- MAC is computed as **CBC residue**
  - That is, **compute CBC encryption**, saving only final ciphertext block, the MAC

# MAC Computation

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- MAC computation (assuming N blocks)

$$C_0 = E(\text{IV} \oplus P_0, K),$$

$$C_1 = E(C_0 \oplus P_1, K),$$

$$C_2 = E(C_1 \oplus P_2, K), \dots$$

$$C_{N-1} = E(C_{N-2} \oplus P_{N-1}, K) = \text{MAC}$$

- **MAC sent with IV and plaintext**
- Receiver does same computation and verifies that result agrees with MAC
- Note: receiver must know the key K

# Does a MAC work?

- Suppose Alice has 4 plaintext blocks
- Alice computes
$$C_0 = E(IV \oplus P_0, K), C_1 = E(C_0 \oplus P_1, K),$$
$$C_2 = E(C_1 \oplus P_2, K), C_3 = E(C_2 \oplus P_3, K) = \text{MAC}$$
- Alice sends  $IV, P_0, P_1, P_2, P_3$  and **MAC** to Bob
- Suppose Trudy changes  $P_1$  to  $X$
- Bob computes
$$C_0 = E(IV \oplus P_0, K), C_1 = E(C_0 \oplus X, K),$$
$$C_2 = E(C_1 \oplus P_2, K), C_3 = E(C_2 \oplus P_3, K) = \text{MAC} \neq \text{MAC}$$
- That is, error propagates into **MAC**
- Trudy can't make **MAC** == **MAC** without  $K$

# Confidentiality and Integrity

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- Encrypt with one key, MAC with another key
- Why not use the same key?
  - Send last encrypted block (MAC) twice?
  - This cannot add any security!
- Using different keys to encrypt and compute MAC works, even if keys are related
  - But, twice as much work as encryption alone
  - Can do a little better —about 1.5 “encryptions”
- Confidentiality and integrity with same work as one encryption is a research topic

# Uses for Symmetric Crypto

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- Confidentiality
  - Transmitting data over insecure channel
  - Secure storage on insecure media
- Integrity (MAC)
- Authentication protocols (later...)
- Anything you can do with a hash function (upcoming chapter...)